Note:

1. All questions are compulsory with internal choice.
2. Draw neat diagrams wherever necessary.
3. Figures to the right indicate full marks.
4. Use of scientific calculator fx 82 series and below is only allowed.

## Q. 1 Answer the following (any EOUR)

(a) Find the interval on which $x^{3}-6 x^{2}+15 x+10$ is increasing or decreasing.
(b) Divide 100 into two parts such that their product is maximum.
(c) By using $\epsilon-\delta$ definition, prove that $\lim _{x \rightarrow 3} \frac{4 x+3}{5}=3$.
(d) Using Newton's method find root of the equation $\mathrm{x}^{3}+4 \mathrm{x}+12=0$ correct upto 4 decimal points. (Take $\mathrm{x}_{0}=-1.5$ )
(e) Find $\frac{\mathrm{dy}}{\mathrm{dx}}$, where $x^{2}+y^{2}=(x+y)^{3}$.
(f) Discuss the continuity of the function in [1,3]. $f(x)= \begin{cases}3 x+2, & x \geq 2 \\ 3 x+4, & x<2\end{cases}$

## Q. 2 Answer the following (any FOUR)

(a) Find area under the curve $y=x^{2}$ and $y=3 x-2$.
(b) Evaluate by using Simpson's method: $\int_{1}^{2} \frac{x}{1+\mathrm{x}^{2}} \mathrm{dx} .($ Take $\mathrm{n}=6)$
(approximate upto 4 decimal).
(c) Solve $: \frac{\mathrm{dy}}{\mathrm{dx}}=(x+y)^{2}$.
(d) Solve by using Euler's method, $\frac{\mathrm{dy}}{\mathrm{dx}}=\mathrm{x}-2 \mathrm{y}, \mathrm{y}(1)=1$. Find $\mathrm{y}(1.2)$. (Take $\left.\mathrm{h}=0.1\right)$
(e) Solve: $\frac{\mathrm{dy}}{\mathrm{dx}}-\frac{1}{x} y=x^{2}$
(f) Evaluate: $\mathrm{I}=\int_{1}^{5} \frac{(\mathrm{x}-2)^{7}}{(\mathrm{x}-2)^{7}+(4-\mathrm{x})^{7}} \mathrm{dx}$
Q. 3 Answer the following (any FOUR)
(a) Using the definition of partial differentiation find $f_{y}$ at $(1,2)$ for $f(x, y)=x+y+x y$
(b) Let $f(x, y, z)=x^{3}+y^{3}+z^{3}+3 x y z$ then find $f_{x y}, f_{z x} \& f_{y z}$.
(c) Find linearization of the following function at (1,2). $f(x, y)=x^{2} y^{2}+x-y+1$.
(d) Find directional derivative of $f(x, y)=x^{2}+2 y^{2}$ at $(1,2)$ in the direction of $(-3,4)$.
(e) Find $\frac{d f}{d t}$, where $f(x, y)=x^{2}-y^{2}$, and $x=1-t^{2}, y=t^{2}$
(f) Find the equation of tangent \& normal to the curve $x^{3}+y^{3}=(x+y)^{2}$ at $(2,2)$

## Q. 4 Answer the following (any EIVE)

(a) Find equation of plane to the curve $2 x^{2}+3 y^{2}-z^{2}-4 y$ at $(1,1,-1)$
(b) Evaluate using Trapizoidal rule: $\int_{5}^{10} x^{2}+1 d x$, (Take $n=5$ )
(c) Check whether the function, $f(x)=\left\{\begin{array}{cc}2 x^{2}+7, & x \geq 1 \\ 4 x+5, & x<1\end{array}\right.$, is differantiable at $\mathrm{x}=1$
(d) Using Newton's method find the approximate value of $\sqrt{23}$. (Take $x_{0}=4.5$ )
(e) Using the definition of partial differentiation find $f_{y}$ at $(1,2)$ for $f(x, y)=x^{3}+y$
(f) Solve the differential equation : $\frac{d y}{d x}=\frac{y+1}{x+1}$

